Write your name here


## Mathematics

Paper 3 (Calculator)
Higher Tier
Mock Set 1 - Autumn 2016
Time: 1 hour 30 minutes
Paper Reference
1MA1/3H

You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

Total Marks


## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided
- there may be more space than you need.
- Calculators may be used.
- If your calculator does not have a $\pi$ button, take the value of $\pi$ to be 3.142 unless the question instructs otherwise.
- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.


## Information

- The total mark for this paper is 80 .
- The marks for each question are shown in brackets - use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


## Answer ALL questions.

## Write your answers in the spaces provided.

## You must write down all the stages in your working.

1 Buses to Ashby leave a bus station every 24 minutes.
Buses to Barford leave the same bus station every 20 minutes.
A bus to Ashby and a bus to Barford both leave the bus station at 730 am .
When will a bus to Ashby and a bus to Barford next leave the bus station at the same time?

2 Amzol thinks that $(x+5)^{2}=x^{2}+25$ for all values of $x$.
Is Amzol right?
You must show how you get your answer.
(Total for Question 2 is $\mathbf{2}$ marks)

3 Kim, Laura and Molly share $£ 385$
The ratio of the amount of money Kim gets to the amount of money Molly gets is $2: 5$ Kim gets $£ 105$ less than Molly gets.

What percentage of the $£ 385$ does Laura get?
\%

4 The table shows information about the heights of 60 trees.

| Height ( $\boldsymbol{h}$ metres) | Frequency |
| :---: | :---: |
| $0<h \leq 4$ | 13 |
| $4<h \leq 8$ | 24 |
| $8<h \leq 12$ | 15 |
| $12<h \leq 16$ | 6 |
| $16<h \leq 20$ | 2 |

Jacob drew this frequency polygon for the information in the table.
The frequency polygon is not correct.


Write down two things that are wrong with the frequency polygon.

1. $\qquad$
2. $\qquad$

5 The price of all rail tickets increased by $5 \%$.
The price of a rail ticket from London to Ipswich increased by $£ 2.30$
Work out the price of the ticket before the increase.

6

$A B C D E$ is a regular pentagon.
$B C F$ and $E D F$ are straight lines.
Work out the size of angle $C F D$.
You must show how you get your answer.
$\qquad$
○

7 A garden is in the shape of a rectangle, $A B C D$, and a semicircle. $A D$ is the diameter of the semicircle.


Carol is going to cover the garden with fertiliser.
A box of fertiliser costs $£ 4.99$
Carol has been told that one box of fertiliser will cover $12 \mathrm{~m}^{2}$ of garden.
(a) Work out the cost of buying enough fertiliser to cover the garden completely.
£ $\qquad$

Carol finds out that one box of fertiliser will cover more than $12 \mathrm{~m}^{2}$ of garden.
(b) Explain how this might affect the number of boxes she needs to buy.
$\qquad$
$\qquad$

8 Sameena has a round pencil case and a square pencil case.
There are 4 blue pens and 3 red pens in the round pencil case.
There are 3 blue pens and 5 red pens in the square pencil case.
Sameena takes at random one pen out of each pencil case.
(a) Complete the probability tree diagram.
round pencil case square pencil case

(2)
(b) Work out the probability that the pens Sameena takes are both red.
$\qquad$

9 Here are six graphs.







Write down the letter of the graph that could have the equation
(i) $y=2^{x}$
(ii) $y=x^{3}-3 x$

10 Simplify $3 m^{2} r \times 4 m^{3} r^{6}$

11 Tom grows tomatoes.
The box plot below shows the distribution of the weights of 15 of Tom's tomatoes.

(a) Work out the interquartile range.
$\qquad$

Jack also grows tomatoes.
Here are the weights, in grams, of 15 of Jack's tomatoes.
$\begin{array}{lllllllllllllll}153 & 155 & 158 & 164 & 166 & 167 & 170 & 170 & 173 & 174 & 175 & 175 & 177 & 179 & 186\end{array}$
(b) On the grid below, draw a box plot for this information.

(c) Compare the distribution of the weights of Tom's tomatoes with the distribution of the weights of Jack's tomatoes.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

12 The diagram shows a piece of wood in the shape of a cuboid.


The piece of wood is 3 cm by 20 cm by 1.2 m .
The mass of the piece of wood is 8 kg .
The piece of wood will float in sea water if the density of the wood is less than the density of the sea water.

In a large pool, 1 litre of sea water has a mass of 1030 g .
Will the piece of wood float in this pool?
You must show how you get your answer.

13 (a) Show that the equation $x^{3}+5 x-4=0$ has a solution between $x=0$ and $x=1$
(b) Show that the equation $x^{3}+5 x-4=0$ can be arranged to give $x=\frac{4}{x^{2}+5}$
(c) Starting with $\quad x_{0}=0$, use the iteration formula $\quad x_{n+1}=\frac{4}{x_{n}{ }^{2}+5}$ twice, to find an estimate for the solution of $x^{3}+5 x-4=0$

14 The number of fish in a lake decreases by $x \%$ each year.
Given that the number of fish halves in 8 years, work out the value of $x$. Give your answer correct to 1 decimal place.

15 Here are two pots.


Pot $\mathbf{A}$ and pot $\mathbf{B}$ are mathematically similar.
The area of the base of pot $\mathbf{B}$ is $160 \mathrm{~cm}^{2}$.
Work out the area of the base of pot $\mathbf{A}$.
$\qquad$ $\mathrm{cm}^{2}$

$$
v=\sqrt{\frac{a}{b}}
$$

$a=6.43$ correct to 2 decimal places.
$b=5.514$ correct to 3 decimal places.
By considering bounds, work out the value of $v$ to a suitable degree of accuracy. Give a reason for your answer.

17 The diagram shows a solid metal cylinder.


The cylinder has base radius $3 x \mathrm{~cm}$ and height $h \mathrm{~cm}$.
The metal cylinder is melted.
All the metal is then used to make 270 spheres.
Each sphere has a radius of $\frac{1}{2} x \mathrm{~cm}$.
Find an expression, in its simplest form, for $h$ in terms of $x$.

18 Make $m$ the subject of

$$
f=\frac{4-3 m}{5+m}
$$

19 The diagram shows a pyramid with base $A B C$.

$C D$ is perpendicular to both $C A$ and $C B$.
Angle $C B D=34^{\circ} \quad$ Angle $A D B=45^{\circ} \quad$ Angle $D B A=60^{\circ}$ $B C=20 \mathrm{~cm}$.

Calculate the size of the angle between the line $A D$ and the plane $A B C$.
Give your answer correct to 1 decimal place.
$\qquad$
.

$$
f(x)=2 x-3 \quad \text { and } \quad g(x)=x^{2}+2
$$

(a) Find $g(-4)$
(b) Show that $\operatorname{gf}(x)=4 x^{2}-12 x+11$
(c) Solve $\operatorname{fg}(x)=\operatorname{gf}(x)$
$A, B, C$ and $D$ are points on the circumference of a circle, centre $O$.


Prove that the sum of angle $A B C$ and angle $A D C$ is $180^{\circ}$

